Section-A : Mathematics

1. If the line $a^2x + ay + 1 = 0$, for some real numbers a, is normal to the curve $xy = 1$
   (a) $a < 0$ (b) $0 < a < 1$
   (c) $a > 0$ (d) $-1 < a < 1$

2. Let Z be the set of all integers, and consider the sets $X = \{(x, y): x^2 + 2y^2 = 3, x, y \in Z\}$ and $Y = \{(x, y): x > y, x, y \in Z\}$. Then the number of elements in $X \cap Y$ is :
   (a) 2   (b) 1   (c) 3   (d) 4

3. The value of the limit $\lim\limits_{x \to 0}\left(\dfrac{1^x + 2^x + 3^x + 4^x}{4}\right)^{\frac{1}{x}}$ is
   (a) 1   (b) $3!^{1/3!}$ (c) $3!^{1/4}$ (d) $4!^{1/4!}$

4. If for non-zero x, $cf(x) + df\left(\dfrac{1}{x}\right) = \big|\log|x|\big| + 3$, where $c \ne d$, then $\displaystyle\int_1^e f(x)\,dx =$
   (a) $\dfrac{(c-d)(2e-1)}{c^2-d^2}$ (b) $\dfrac{(c-d)(3e-2)}{c^2-d^2}$
   (c) $\dfrac{(c-d)(3e+2)}{c^2-d^2}$ (d) $\dfrac{(c-d)(2e+1)}{c^2-d^2}$

5. If $x = 1 + \sqrt[6]{2} + \sqrt[6]{4} + \sqrt[6]{8} + \sqrt[6]{16} + \sqrt[6]{32}$, then $\left(1 + \dfrac{1}{x}\right)^{24} =$
   (a) 1   (b) 4   (c) 16   (d) 24

6. Out of a group of 50 students taking examinations in Mathematics, Physics, and Chemistry, 37 students passed Mathematics, 24 passed Physics, and 43 passed Chemistry. Additionally, no more than 19 students passed both Mathematics and Physics, no more than 29 passed both Mathematics and Chemistry, and no more than 20 passed both Physics and Chemistry. What is the maximum number of students who could have passed all three examinations?
   (a) 10   (b) 9   (c) 14   (d) 12

7. The points (1,1/2) and (3,-1/2) are
   (a) In between the lines 2x+3y=6 and 2x+3y = -6
   (b) On the same side of the line 2x+3y = 6
   (c) On the opposite side of the line 2x+3y = -6
   (d) On the same side of the line 2x+3y = -6

8. A speaks truth in 40% and B in 50% of the cases. The probability that they contradict each other while narrating some incident is:
   (a) 1/2   (b) 1/4   (c) 2/3   (d) 1/3

9. Let $f(x) = \begin{cases} x^2 \sin\dfrac{1}{x}, & x \ne 0 \\ 0, & x = 0 \end{cases}$
   Then which of the following is true
   (a) f(x) is not continuous at x = 0
   (b) f(x) is not differentiable at x = 0
   (c) f'(x) is not continuous at x = 0
   (d) f'(x) is continuous at x = 0

10. At how many points the following curves intersect
    $\dfrac{y^2}{9} - \dfrac{x^2}{16} = 1$ and $\dfrac{x^2}{4} + \dfrac{(y-4)^2}{16} = 1$
    (a) 0   (b) 1   (c) 2   (d) 4

11. Among the given numbers below, the smallest number which will be divided by 9, 10, 15 and 20, leaves the remainders 4, 5, 10, and 15, respectively
    (a) 535   (b) 355   (c) 265   (d) 85

12. Lines $L_1, L_2, \ldots, L_{10}$ are distinct among which the lines $L_2, L_4, L_6, L_8, L_{10}$ are parallel to each other and the lines L_1, L_3, L_7, L_9 pass through a given point C. The number of point of intersection of pairs of lines from the complete set $L_1, L_2, L_3, \ldots, L_{10}$, is
    (a) 24   (b) 25   (c) 26   (d) 27

13. The value of m for which volume of the parallelepiped is 4 cubic units whose three edges are represented by $a = mi + j + k$, $b = i - j + k$, $c = i + 2j - k$ is
    (a) 0   (b) -2   (c) -1   (d) 1

14. The equation $3x^2 + 10xy + 11y^2 + 14x + 12y + 5 = 0$
    (a) a circle   (b) an ellipse
    (c) a hyperbola   (d) a parabola

15. Consider the function $f(x) = x^{2/3}(6-x)^{1/3}$. Which of the following statement is FALSE?
    (a) f is increasing in the interval (0, 4)
    (b) f is decreasing in the interval (6, ∞)
    (c) f has a point of inflection at x = 0
    (d) f has a point of inflection at x = 6

16. Which of the following is TRUE?
    (a) If f is continuous on [a, b], then
    $$\int_a^b xf(x)\,dx = x\int_a^b f(x)\,dx$$
    (b) $\displaystyle\int_0^2 e^{x^2}\,dx = \int_0^5 e^{x^2}\,dx + \int_5^3 e^{x^2}\,dx$
    (c) If f is continuous on [a, b], then
    $$\frac{d}{dx}\left(\int_a^b f(x)\,dx\right) = f(x)$$
    (d) Both (a) and (b)

17. Let $f : R \to R$ be a function such that $f(0) = \dfrac{1}{\pi}$ and $f(x) = \dfrac{x}{e^{\pi x} - 1}$ for $x \ne 0$
    Then
    (a) f(x) is not continuous at x = 0
    (b) f(x) is continuous but not differentiable at x = 0
    (c) f(x) is differentiable at x = 0 and $f'(0) = -\dfrac{\pi}{2}$
    (d) None of the above

18. If the perpendicular bisector of the line segment joining p(1,4) and q(k,3) has y-intercept -4, then the possible values of k are
    (a) -4 and 4   (b) -2 and 2
    (c) -1 and 1   (d) -3 and 3

19. A coin is thrown 8 number of times. What is the probability of getting a head in an odd number of throw?
    (a) 1/8   (b) 3/4   (c) 1/2   (d) 1/4

20. The number of one-one functions $f : \{1, 2, 3\} \to \{a, b, c, d, e\}$ is
    (a) 125   (b) 60
    (c) 243   (d) None of the above

21. The value of f(1) for $f\left(\dfrac{1-x}{1+x}\right) = x + 2$ is
    (a) 1   (b) 2   (c) 3   (d) 4

22. The number of distinct real values f λ for which the vectors $\lambda^2\hat{i}+j+k, \hat{i}+\lambda^2 j+k$, and $\hat{i}+j+\lambda^2 k$ are coplanar is
(a) 1   (b) 2   (c) 3   (d) 6

23. How much work does it take to slide a crate for a distance of 25 m along a loading dock by pulling on it with a 180 N force where the dock is at an angle of 45° from the horizontal?
(a) 3.18198×10^3J   (b) 3.18198×10^2J
(c) 3.4341×10^3J   (d) 3.4341×10^4J

24. If f(x) = cos [π^2]x + cos[-π^2]x, where [.] stands for the greatest integer function, then f($\pi/2$) =
(a) – 1   (b) 0   (c) 1   (d) 2

25. It is given that the mean, median and mode of a data set is 1, 3^x and 9^x respectively. The possible values of the mode is
(a) 1, 4   (b) 1, 9   (c) 3, 9   (d) 9, 8

26. If |F| = 40N (Newtons), |D| = 3m, and θ = 60°, then the work done by F acting from P to Q is
(a) $60\sqrt{3}$J   (b) 120J   (c) $60\sqrt{2}$J   (d) 60J

27. The vector $\vec{A} = (2x+1)\hat{i} + (x^2-6y)j + (xy^2+3z)k$
is a
(a) sink field   (b) solenoidal field
(c) source field   (d) none of these

28. If one AM (Arithmetic mean) 'a' and two GM's (Geometric means) p and q be inserted between any two positive numbers, the value of $p^3 + q^3$ is
(a) 2apq   (b) pq/a   (c) 2pq/a   (d) p+q+a

29. A committee of 5 is to be chosen from a group of 9 people. The probability that a certain married couple will either serve together or not at all is
(a) 4/9   (b) 5/9   (c) 1/2   (d) 2/3

30. If three distinct numbers are chosen randomly from the first 100 natural numbers, then the probability that all three of them are divisible by both 2 and 3 is
(a) 4/33   (b) 4/1155   (c) 4/25   (d) 4/35

31. The system of equations x + 2y + 2z = 5, x + 2y + 3z = 6, x + 2y + λz = μ has infinitely many solutions if
(a) $\lambda \neq 2$ (b) $\lambda \neq 2$, $\mu \neq 5$
(c) $\lambda = 2$, $\mu = 5$ (d) $\mu \neq 5$

32. For an invertible matrix A, which of the following is not always true:
(a) $|adj (A)| \neq 0$ (b) $|A| \neq 0$
(c) $|AA^{-1}| = 1$ (d) $|A(adj(A))| \neq 1$

33. If sin x = sin y and cos x = cos y, then the value of x – y is
(a) $\pi/4$ (b) $n\pi/2$ (c) $n\pi$ (d) $2n\pi$

34. The value of series $\frac{2}{3!}+\frac{4}{5!}+\frac{6}{7!}+............$, is
(a) $2e^{-2}$ (b) e^{-2} (c) e^{-1} (d) $2e^{-1}$

35. Find the cardinality of the set C which is defined as
$C\{x \mid \sin 4x = \frac{1}{2}$ for x $\in (-9\pi, 3\pi)\}$.
(a) 24   (b) 48   (c) 36   (d) 12

36. For what values of λ does not equation $6x^2 – xy + \lambda y^2 = 0$ represents two perpendicular lines and two lines inclined at an angle of $\pi/4$.
(a) – 6 and – 2   (b) 6 and 1
(c) – 6 and – 35   (d) – 6 and 1

37. The number of solutions of $5^{1+|\sin x|+|\sin x|^2+........} = 25$ for x $\in (-\pi, \pi)$ is

38. Given a set A with median $m^1 = 2$ and set B with median $m^2 = 4$ What can we say about the median of the combined set?
(a) 2   (b) 0   (c) 4   (d) ∞
(a) at most 1   (b) at most 2
(c) at least 1   (d) at least 2

39. There are 9 bottle labeled 1, 2, 3, ……., 9 and 9 boxes labeled 1, 2, 3, ……, 9. The number of ways one can put these bottles in the boxes so that each box gets one bottle and exactly 5 bottles go in their corresponding numbered boxes is
(a) $9 \times {}^9C_5$ (b) $5 \times {}^9C_5$
(c) $25 \times {}^9C_5$ (d) $4 \times {}^9C_5$

40. A critical orthopedic surgery is performed on 3 patients. The probability of recovering a patient is 0.6. Then the probability that after surgery, exactly two of them will recover is
(a) 0.432   (b) 0.234   (c) 0.321   (d) 0.123

41. A man starts at the origin O and walks a distance of 3 units in the north-east direction and then walks a distance of 4 units in the north-west direction to reach the point P. then $\overline{OP}$ is equal to
(a) $\frac{1}{\sqrt{2}}(-\hat{i}+j)$ (b) $\frac{1}{2}(\hat{i}+j)$
(c) $\frac{1}{\sqrt{2}}(\hat{i}-7j)$ (d) $\frac{1}{\sqrt{2}}(-\hat{i}+7j)$

42. Consider the function
$f(x) = \begin{cases} -x^3+3x^2+1, & if\ x \leq 2 \\ \cos(x), & if\ 2 < x \leq 4 \\ e^{-x}, & if\ x > 4 \end{cases}$
Which of the following statements about f(x) is true:
(a) f(x) has a local maximum at x = 1, which is also the global maximum.
(b) f(x) has a local maximum at x = 2, which is not the global maximum.
(c) f(x) has a local maximum at x = π, but it is not the global maximum.
(d) f(x) has a global maximum at x = 0.

43. The value of $\tan\left(\frac{\pi}{4}+\theta\right)\tan\left(\frac{3\pi}{4}+\theta\right)$ is
(a) – 2   (b) 2   (c) 1   (d) – 1

44. Let A and B be two events defined on a sample space Ω Suppose A^c denotes the complement of A relative to the sample space Ω. Then the probability $P((A \cap B^c) \cup (A^c \cap B))$ equals
(a) $P(A) + P(B) + P(A \cap B)$
(b) $P(A) + P(B) - P(A \cap B)$
(c) $P(A) + P(B) + 2P(A \cap B)$
(d) $P(A) + P(B) - 2P(A \cap B)$

45. The value of $\lim_{x \to 0} \frac{e^x - e^{-x} - 2x}{1 - \cos x}$ is equal to
(a) 2   (b) 1   (c) 0   (d) – 1

46. Let C denote the set of all tuples (x, y) which satisfy $x^2 – 2^y$ where x and y are natural numbers. What is the cardinality of C?
(a) 0   (b) 1   (c) 2   (d) 3

47. The two parabolas $y^2 = 4a(x + c)$ and $y^2 = 4bx$, a > b > 0 cannot have a common normal unless
(a) c > 2 (a + b)   (b) c > 2(a – b)

(c) $c < 2(a - b)$ (d) $c < \dfrac{2}{a-b}$

48. If (4, 3) and (12, 5) are the two foci of an ellipse passing through the origin, then the eccentricity of the ellipse is

(a) $\dfrac{\sqrt{13}}{9}$ (b) $\dfrac{\sqrt{13}}{18}$ (c) $\dfrac{\sqrt{17}}{18}$ (d) $\dfrac{\sqrt{17}}{9}$

49. The value of $\displaystyle\sum_{r=1}^{n} \dfrac{1}{2^n} \dfrac{{}^n P_r}{r!}$

(a) 2^n (b) $1 - 2^{-n}$ (c) $2^n - 1$ (d) $2^{2n} - 1$

50. Region R is defined as region in first quadrant satisfying the condition $x^2 + y^2 < 4$. Given that a point $P = (r, s)$ lies in R, what is the probability that $r > s$?

(a) 1 (b) 0 (c) 1/2 (d) 1/3

Section-B : Analytical Ability & Logical Reasoning

1. Select the one which is different from the other three.
(a) JGP (b) HEM (c) NKS (d) OLT

2. Four friends Aditi, Bharat, Chandan, and Deepika, went to a restaurant for dinner. Each of them ordered a different dish from the menu: pizza, pasta, burger, and salad. Additionally, each friend ordered a different drink: cola, lemonade, orange juice, and water. Based on the following clues, determine the combination of friend, dish, and drink:
Aditi didn't order pizza and cola.
Bharat ordered salad but not lemonade.
Chandan ordered pasta.
Deepika didn't order burger or orange juice.
Aditi ordered orange juice.
Who ordered the burger, and what drink did they order?
(a) Chandan, lemonade (b) Aditi, orange juice
(c) Deepika, cola (d) Bharat, water

3. A cat climbs a 21-meter pole. In the first minute it climbs 3 meter and in the second minute it descends one meter. In how minutes the cat would reach the top of the pole?
(a) 20 minutes (b) 19 minutes
(c) 18 minutes (d) 21 minutes

4. Study the following diagram and answer the following question.
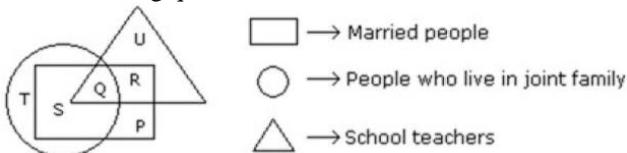
By which letter, the married teachers who do not live in joint family are represented?
(a) R (b) P (c) Q (d) S

5. Rajesh will not go to the concert if Rakesh goes. Rakesh will go to the concert if his dog barks three times.
Based only on the information above, which of the following must be true?
(a) If Rakesh's dog does not bark three times, then Rakesh will not go to the concert.
(b) If Rakesh's dog barks three times, then Rajesh will not go to the concert.
(c) If Rajesh doesn't go to the concert, then Rakesh will go.

(d) Rakesh will not go to the concert unless Rajesh goes.

6. Select the pair of words, which are related in the same way as the capitalized words are related to each other.
DATA : GRAPH
(a) Mother : Father (b) Plant : Leaf
(c) Milk : Butter (d) Water : Glass

7. If by rearranging the letters of the word NABMODINT, a name of a game is formed. What would be the first and last letter of the mirror image of the name of the game?
(a) B, T (b) N,B (c) B,N (d) T,B

8. In certain languages, HEART is written as 2018010508, and LUNGS is written as 1907142112. If BRAIN is written in that language, what will be the last number?
(a) 2 (b) 4 (c) 9 (d) 5

9. In a reality show, two judges independently provided marks based on the performance of the participants. If the marks provided by the second judge are given by $Y = 10.5 + 2X$, where X is the marks provided by the first judge. If the variance of the marks provided by the second judge is 100, then the variance of the marks provided by the first judge is:
(a) 25 (b) 50 (c) 49.5 (d) 99

10. Aryan bought 100 shares of a company at Rs. 50 per share. He paid a brokerage fee of 2% on the purchase. Later, he sold all the shares at Rs. 55 per share and paid a brokerage fee of 2% on the sale. What is Aryan's net profit percentage on his investment?
(a) 5.69% (b) 5.5% (c) 6% (d) 6.1%

11. Which out of the following words will appear last in the dictionary
(a) Compliment (b) Complicit
(c) Compline (d) Complete

12. After allowing 20% cash discount, a trader still earns a profit of 11.11%. How much above the cost price, the trader marks his goods?
(a) 28% (b) 30.33%
(c) 38.88% (d) 40%

13. If 30th September, 1991 was a Wednesday, then what was the day on 14th March 1992?
(a) Sunday (b) Saturday
(c) Monday (d) Wednesday

14. Looking at the portrait of a man, Lucky (male) said, "This person is the only child of my paternal grandmother's daughter." Whose portrait was Lucky looking at?
(a) His uncle (b) His cousin
(c) Himself (d) His brother

15. In which year was Arjun born?
Arjun at present is 25 years younger to his mother. Arjun's brother, who was born in 1964, is 35 years younger to his mother.
(a) 1974 (b) 1964 (c) 1944 (d) 1954

16. What is the value of $x^2 + y^2 = ?$
Statement I : $xy = 5$
Statement II : $x + y = 10$
(a) Choose this option if the question can be answered by using one of the statements alone, but cannot be answered using the other statement

(b) Choose this option if the question can be answered by using both the statements together, but cannot be answered using either statement alone.

(c) Chose this option if the question can be answered by using either statement alone

(d) Choose this option if the question cannot be answered even by using both the statements together

17. You are on an island with two tribes. One tribe always tells the truth, and the other tribe always lies. You meet three individuals from the island: A, B and C. Each individual belongs to one of the tribes. You ask each of them the same question: "is B a truth-teller?"

Here are their responses:

A says, "Yes, B is a truth-teller."

B says, "No, I am not a truth-teller."

C says, "B is a liar."

Given that each individual is either a truth-teller or a liar, who is telling the truth?

(a) B only   (b) C only

(c) Both B and C   (d) A only

18. Which pairs of bits can be joined together to form two words that have opposite meanings?

ERT	UCE	DES	END	EXP	EAR	AND	SIP	RED	GOS
1	2	3	4	5	6	7	8	9	10

(a) (9, 2), (5, 7)   (b) (1, 3), (8, 10)

(c) (1, 5), (10, 8)   (d) (4, 2), (7, 8)

19. Odometer is to mileage as Compass is to

(a) Hiking   (b) Needle

(c) Speed   (d) Direction

20. The mean of consecutive positive integers from 2 to n is

(a) $\dfrac{n+2}{2}$ (b) $\dfrac{n(n+1)}{2}$ (c) $\dfrac{n+1}{2}$ (d) $\dfrac{n-1}{2}$

21. Study the following information carefully and answer the given question:

Eight friends A, B, C, D, E, F, G, and H are sitting on a round table facing the centre. A sits second to the left of D, who sits third to the left of E. C sits third to the right of G, who is not an immediate neighbour of E. H sits opposite to the E. B is between A and C.

Who sits opposite to A?

(a) G   (b) E   (c) D   (d) F

22. This question contains six statements followed by four sets of combinations of three. Choose the set in which the combinations are most logically related.

A. Some building are not skyscrapers

B. Some skyscrapers are not buildings

C. No structure is a skyscraper

D. All skyscrapers are structures

E. Some skyscrapers are buildings

F. Some structures are not buildings

(a) ACF   (b) BDF   (c) ACE   (d) FDA

23. Which one of the following is the odd one from the given alternative?

(a) Salary   (b) Years of experience

(c) Age   (d) Highest education

24. This question contains six statements followed by four sets of combinations of three. Choose the set in which the combinations are most logically related.

A. All falcons fly high   B. All falcons are blind

C. All falcons are birds   D. All birds are yellow

E. All birds are thirsty   F. All falcons are yellow.

(a) BCA   (b) ABC   (c) DEF   (d) CDF

25. In the following question, three statements and three conclusions are given.

Statements: 1. All students are intelligent.

2. No intelligent person is lazy.

3. Some lazy people are poor

Conclusions: 1. No student is lazy.

2. Some poor people are not intelligent.

3. All poor people are lazy.

Find out the most appropriate conclusion(s) from the following options.

(a) Only conclusion 2 follows

(b) Only conclusion 1 follows

(c) Only conclusions 2 and 3 follow

(d) Only conclusions 1 and 2 follow

26. At what time between 2 pm and 3 pm, will the hour and minute hands of a clock point in opposite directions (diametrically opposite)?

(a) 2:45 pm   (b) 2:44 pm

(c) $2:43\dfrac{9}{11}$ pm   (d) $2:43\dfrac{7}{11}$ pm

27. Two cars, Car A and Car B, are traveling on a highway. Car A starts from point X and travels at a constant speed of 60 km/h, while Car B starts from the same point X but travels at a constant speed of 80 km/h. If both cars travel for 1.5 hours, what is the difference in distance covered by Car B compared to Car A?

(a) 20 KM (b) 30 KM (c) 25 KM (d) 35 KM

28. In the half yearly exam only 60% of the students were passed. Out of these (passed in halfyearly) only 70% students are passed in annual exam, out of remaining students (who fail in half-yearly exam) 80% passed in annual exam. What percent of the students passed the annual exam?

(a) 74%   (b) 72%   (c) 76%   (d) 65%

29. Arrange the words given below in a meaningful sequence.

(1)Software (2) Code (3) Data (4) Analysis (5) Report

(a) 3, 1, 2, 4, 5   (b) 5, 4, 3, 1, 2

(c) 2, 1, 5, 3, 4   (d) 3, 1, 2, 5, 4

30. In a tournament, many teams participated. All teams in the tournament have 5 to 15 players.

If a team has more than 10 players, then they have reversible t-shirts.

Based only on the information above, which of the following must be true?

(a) Teams that have 12 players do not have reversible t-shirts.

(b) Only people on teams can have reversible t-shirts.

(c) Teams with 8 players do not have reversible t-shirts.

(d) Teams that have 13 players have reversible t-shirts.

31. Ramu visits Delhi on every 15 days and Samu goes to Delhi every 20 days. They met at Delhi 5 days back. After how many days, from today, they will meet at Delhi next time?

(a) 35   (b) 65   (c) 60   (d) 55

32. In a recent survey of 500 employees in a company, it was found that 60% of the employees prefer coffee over tea, 25% prefer tea over coffee, and the remaining 15% have no preference. If 20% of the

employees who prefer coffee are also tea drinkers, how many employees prefer only tea?
(a) 75 (b) 65 (c) 50 (d) 55

33. From the given options, find the pair which is like the given pair 8:4
(a) 216:32 (b) 45:5 (c) 72:24 (d) 27:9

Comprehension:

Directions : A, B, C, D, E, F and G are travelling in three different vehicles. There are at least two passengers in each vehicle – Swift, Creta, Nexon, and only one of them is a male. There are two engineers, two doctors and three teachers among them.
  i. C is a lady doctor and she does not travel with the pair of sisters A and F.
  ii. B, is a male engineer, travels with only G, a teacher in a Swift.
  iii. D is a male doctor
  iv. Two persons belonging to the same profession do not travel in the same vehicle.
  v. A is not an engineer and travels in a Creta.
  vi. The pair of sisters A and F travel in the same vehicle.

34. What is F's profession?
(a) Data inadequate   (b) Teacher
(c) Doctor   (d) Engineer

35. In which vehicle does C travel?
(a) Creta (b) Swift (c) Nexon (d) Data inadequate

36. Which of the following represents the three teachers?
(a) GEA (b) GEF (c) GBF (d) Data inadequate

Comprehension:

Direction: A, B, C, D and E are five different integer. When written in the ascending order of values, the difference between any two adjacent integers is 8. D is the greatest and A the least. B is greater than E but less than C. The sum of the integers is equal to E.

37. The value of A is:
(a) -17 (b) -18 (c) -15 (d) None of these

38. The sum of A and B is:
(a) -30   (b) -20
(c) None of these   (d) -15

39. The greatest number has the value:
(a) 12 (b) 17 (c) 15 (d) 14

40. The sum of the integers is:
(a) -6   (b) -10
(c) None of these   (d) -8

Section-C : Computer Awareness and English

1. Cache memory functions as an intermediary between
(a) RAM and ROM   (b) CPU and RAM
(c) None of these   (d) CPU and Hard Disk

2. Which of the following is the smallest unit of data in a computer?
(a) KB   (b) Nibble
(c) Byte   (d) Bit

3. The range of the exponent E in the IEEE754 double precision (Binary64) format is _____
(a) $-1022 \leq E \leq 1023$ (b) $-1022 \leq E \leq 1022$
(c) $-1023 \leq E \leq 1022$ (d) $-1023 \leq E \leq 1023$

4. Which of the following components is used to establish a communication link between a CPU and the peripheral devices to transfer data?
(a) Memory address register
(b) Memory data register
(c) Index register
(d) Instruction register

5. Which of the following do not affects CPU performance?
(a) Number of cores   (b) Amount of RAM
(c) Clock speed   (d) Cache size

6. Any given truth table can be represented by
(a) a sum of product Boolean expression
(b) a Karnaugh map
(c) All of the options
(d) a product of sum Boolean expression

7. The Boolean expression for the following truth table is _____

x	y	z	f
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1

(a) F = x'yz'+xy'z+x'y'z   (b) F = x'yz'+xy'z+xyz'
(c) F = x'yz'+xy'z+xyz   (d) None of these

8. Which of the following interfaces perform the transfer of data between the memory and the I/O peripheral without involving the CPU?
(a) Serial Interface   (b) DMA
(c) Branch Interface   (d) DDA

9. Consider the program below which uses six temporary variables a, b, c, d, e, and f.
```
a = 10
b = 20
c = 30
d = a+c
e = b+d
f = c+e
b = c+e
e = b+f
d = 5+e
return d+f
```
Assuming that all the above operations take their operands from registers, the minimum number of registers needed to execute this program without spilling is _____
(a) 3   (b) 6   (c) 5   (d) 4

10. Let the given numbers 11001, 1001 and 111001 be correspond to the 2's complement representation. Then with which one of the following decimal numbers, the given numbers match?
(a) -25, -9 and -57, respectively
(b) 25, 9 and 57, respectively
(c) -7, -7, and -7, respectively
(d) -6, -6, and -6, respectively

11. A computer system has 16-bit wide address/data bus that uses RAM chips of 4K x 8-bit capacity. The number of RAM chips are needed to provide a memory capacity of 64 Kbytes memory is ___
(a) 64   (b) 32   (c) 16   (d) 8

12. In the figure, the circle stands for employed, the square stands for a social worker, the triangle stands for illiterate, and the rectangle stands for truthful. Study the figure with its regions and find the number of neither truthful nor illiterate people among the employed only.
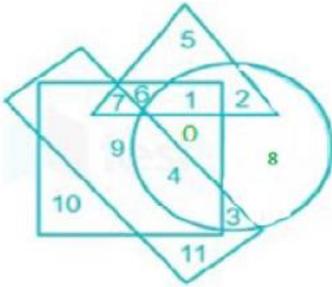
(a) 11   (b) 1   (c) 8   (d) 4

13. The primary purpose of cache memory in a computer system is
(a) to temporarily store frequently accessed data and instructions for faster access by the CPU
(b) to permanently store data and programs
(c) to provide additional storage space when the main memory is full
(d) to manage input and output operations between the CPU and peripherals

14. Consider the following 4-bit binary numbers represented in the 2's complement form: 1101 and 0100.
What would be the result when we add them?
(a) 0001 and an overflow   (b) 0001 and no overflow
(c) 1001 and an overflow   (d) 1001 and no overflow

15. Consider an arbitrary number system with independent digits as 0, 1 and A. If we generate first few numbers in sequence as 00, 01, 0A, 10, 11, 1A and if this process is continued to generate the numbers, then the position of 10A is ____
(a) 12   (b) 9   (c) 10   (d) 15

16. A CPU generates 32 bits virtual addresses. The page size is 4 KB. The processor has a translation look-aside buffer (TLB) which can hold a total of 128-page table entries and is 4- way set associate. The minimum size of the TLB tag is
(a) 15 bits   (b) 20 bits
(c) 13 bits   (d) 11 bits

17. Which of the following components is not a part of an instruction format in CPU processing?
(a) Register file   (b) Source operand
(c) Destination operand   (d) Opcode

18. The quotient, if the binary number 11010111 is divided by 101, is _____
(a) 101101   (b) 111001
(c) 101010   (d) 101011

19. Given that numbers A and B are two 8 bit 2's Complement numbers with A=11111111; B=11111111. Then sum A+B is _____
(a) 00000000   (b) 00000010
(c) 11111100   (d) 11111110

20. The expression P+QR is the reduced form of _____
(a) (P+Q)(P+R)   (b) (P+Q)R
(c) PQ + QR   (d) (P+R)Q

21. Identify the word that means the same as "ostentatious":
(a) Simple   (b) Modest
(c) Lavish   (d) Unassuming

22. Write the antonym for 'Inscrutable':
(a) Obscure   (b) Mysterious
(c) Comprehensible   (d) Opaque

23. Which sentence demonstrates correct preposition usage?
(a) They were surprised of the sudden announcement.
(b) I prefer coffee over tea.
(c) He is interested on learning new languages.
(d) She arrived to the party at 8 PM.

24. Select the correct meaning of 'Peruse':
(a) Continue   (b) Pursue
(c) Examine   (d) Rescue

25. Choose the correct combination of prepositions to complete the sentence:
"The cat jumped ___ the table ___ the chair."
(a) off, in   (b) onto, towards
(c) into, beside   (d) on, from

26. What does the idiom "jump on the bandwagon" mean?
(a) To repair a vehicle
(b) To join a popular trend or activity
(c) To start a business
(d) To criticize something unfairly

27. Choose the best option that indicates the change of voice for the sentence given below:
Did Alice invite you?
(a) Did you invited by Alice?
(b) Were you invited by Alice?
(c) Was Alice invited you?
(d) Had you invited Alice?

28. The company's _____ growth in revenue surprised analysts.
(a) exponential   (b) stagnant
(c) erratic   (d) gradual

29. Select the appropriate synonym for 'coercive':
(a) Corrective   (b) Forceful
(c) Merciful   (d) Gentle

30. Which of the following is an essential element of a technical report?
(a) Emotional appeals
(b) Creative storytelling
(c) Statistical data and analysis
(d) Anecdotes and personal opinions

NIMCET-2024 ANSWERS

1	2	3	4	5	6	7	8	9	10
a	b	d	b	c	c	a	a	c	c
11	12	13	14	15	16	17	18	19	20
b	c	d	b	c	b	d	a	c	b
21	22	23	24	25	26	27	28	29	30
b	b	a	a	a	d	a	a	a	b
31	32	33	34	35	36	37	38	39	40
c	d	d	c	b	c	c	d	a	a
41	42	43	44	45	46	47	48	49	50
d	b	d	d	c	c	b	d	b	c

1	2	3	4	5	6	7	8	9	10
a	b	b	a	b	c	b	a	a	a
11	12	13	14	15	16	17	18	19	20
c	c	c	b	d	b	b	a	d	a
21	22	23	24	25	26	27	28	29	30
d	b	d	d	d	d	b	a	a	d
31	32	33	34	35	36	37	38	39	40
d	b	d	d	c	a	b	b	d	b

1	2	3	4	5	6	7	8	9	10
b	d	a	b	B	c	c	b	a	c
11	12	13	14	15	16	17	18	19	20
c	c	a	b	b	a	a	d	d	a
21	22	23	24	25	26	27	28	29	30
c	c	b	c	b	b	b	a	b	c

1. **Ans. (a)** Here curves are $a^2x + ay + 1 = 0$ and $xy = 1$

$$a^2 + \frac{ady}{dx} = 0 \Rightarrow \frac{dy}{dx} = -a = m_1$$

$$xy = 1 \Rightarrow y = \frac{1}{x} \Rightarrow \frac{dy}{dx} = -\frac{1}{x^2} = m_2$$
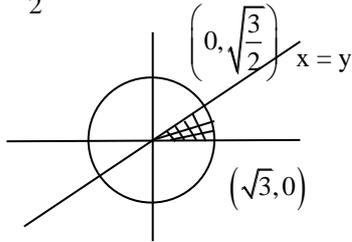
$$m_1 m_2 = -1$$

$$\Rightarrow \frac{a}{x^2} = m_1 m_2 = -1$$

$$\Rightarrow x^2 = -a$$

As $x^2 > 0 \Rightarrow -a > 0 \Rightarrow a < 0$

2. **Ans. (b)** $x : x^2 + 2y^2 = 3,\ x, y \in z$

$$\frac{x^2}{3} + \frac{y^2}{\frac{3}{2}} = 1$$

$$X \cap Y = \{(1,0)\} \text{ as } x > y$$

$$\Rightarrow N(X \cap Y) = 1$$

3. **Ans. (d)** $\displaystyle \lim_{x \to 0} \left(\frac{1^x + 2^x + 3^x + 4^x}{4} \right)^{\frac{1}{x}}$

$$= \lim_{x \to 0} \left(1 + \frac{(1^x - 1) + (2^x - 1) + (3^x - 1) + (4^x - 1)}{4} \right)^{\frac{1}{x}\left(\frac{1^x-1}{4}+\frac{2^x-1}{4}+\frac{3^x-1}{4}+\frac{4^x-1}{4}\right) \times \frac{4}{(1^x-1)+(2^x-1)+(3^x-1)+(4^x-1)}}$$

$$e^{\frac{1}{4}\lim_{x\to0}\frac{1^x-1}{x}+\frac{2^x-1}{x}+\frac{3^x-1}{x}+\frac{4^x-1}{4}}$$

$$e^{\frac{1}{4}[\log_e 1 + \log_e 2 + \log_e 3 + \log_e 4]}$$

$$e^{\frac{1}{4}\log_e(1.2.3.4)} = (24)^{\frac{1}{4}}$$

4. **Ans. (b)** $cf(x) + df\left(\frac{1}{x}\right) = \left|\log|x|\right| + 3$

Put $x = \frac{1}{x}$

$$cf\left(\frac{1}{x}\right) + df(x) = \left|\log\left|\frac{1}{x}\right|\right| + 3$$

$$= \left|\log\left|\frac{1}{x}\right|\right| + 3$$

$$\Rightarrow cf(x) + df\left(\frac{1}{x}\right) = cf\left(\frac{1}{x}\right) + df(x)$$

$$\Rightarrow c\left[f(x) - f\left(\frac{1}{x}\right)\right] d\left[f(x) - f\left(\frac{1}{x}\right)\right] = 0$$

$$\Rightarrow c = d \text{ or } f(x) = f\left(\frac{1}{x}\right)$$

But $c \neq d \Rightarrow f(x) = f\left(\frac{1}{x}\right)$

$$\Rightarrow cf(x) + df(x) = \left|\log|x|\right| + 3$$

$$\Rightarrow f(x)[c + d] = |\log|x|| + 3$$

$$f(x) = \frac{1}{c+d}[\left|\log|x|\right| + 3]$$

$$\Rightarrow \int_1^e f(x)\,dx = \frac{1}{c+d}\int_1^e (\left|\log|x|\right| + 3)\,dx$$

$$= \frac{1}{c+d}\int_1^e (\log x + 3)\,dx \text{ as } 1 < x < e \Rightarrow |x| = x$$

$|\log |x|| = \log x$

$$= \frac{1}{c+d}[x\log x - x + 3x]_1^e$$

$$= \frac{1}{c+d}[(e - e + 3e) - [-1 + 3]] = \frac{3e-2}{c+d}$$

$$= \frac{(3e-2)(c-d)}{c^2 - d^2}$$

5. **Ans. (c)** $x = 1 + 2^{\frac{1}{6}} + 2^{\frac{2}{6}} + 2^{\frac{3}{6}} + 2^{\frac{4}{6}} + 2^{\frac{5}{6}}$

G.P with $a = 1, r = 2^{\frac{1}{6}}$

$$x = \frac{1(1 - (2^{\frac{1}{6}})^6)}{1 - 2^{\frac{1}{6}}} = \frac{1-2}{1-2^{\frac{1}{6}}} = \frac{-1}{1-2^{\frac{1}{6}}}$$

$$1 - 2^{+\frac{1}{6}} = -\frac{1}{x}$$
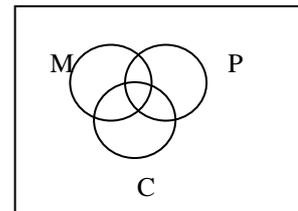
$$1 + \frac{1}{x} = 2^{+\frac{1}{6}}$$

$$\left(1 + \frac{1}{x}\right)^{24} = (2^{+\frac{1}{6}})^{24} = 2^{+4} = 16$$

6. **Ans. (c)** $n(M) = 37, n(P) = 24^n, (C) = 43$

$$n(M \cap P) \leq 19, n(M \cap C) \leq 29$$

$$n(P \cap C) \leq 20$$

$$n(M \cap P \cap C) \leq ?$$

As

$$n(M \cup P \cup C) = n(M) + n(P) + n(C)$$

$$- n(M \cap P) - n(M \cap C)$$

$$- n(P \cap C) + n(P \cap P \cap C)$$

$$50 \geq 37 + 24 + 43 - 19 - 29 - 20 + n(M \cap P \cap C)$$

$$n(M \cap P \cap C) \leq 50 - 36 = 14$$

7. **Ans. (a)** Points are A $\left(1, \frac{1}{2}\right)$ and B $\left(3, \frac{-1}{2}\right)$

$L_1 : 2x+3y-6=0, L_2 : 2x+3y+6=0$

For A $\left(1, \frac{1}{2}\right) \Rightarrow L_1 : 2.1 + 3.\frac{1}{2} - 6 < 0$

$L_2 : 2(1) + 3(\frac{1}{2}) + 6 > 0$

$\Rightarrow \left(1, \frac{1}{2}\right)$ lie between L_1, L_2

Also for B $\left(3, -\frac{1}{2}\right)$

$L_1 : 2(3) + 3(-\frac{1}{2}) - 6 < 0$

$L_2 : 2(3) + 3(-\frac{1}{2}) + 6 > 0$

$\Rightarrow B\left(3, -\frac{1}{2}\right)$ lie b/w L_1, L_2

So (1)true
Now for $2x+3y=6$

$A\left(1, \frac{1}{2}\right), B\left(3, -\frac{1}{2}\right)$

$\Rightarrow 2(1) + \frac{3}{2} - 6 < 0$

$2(3) + 3\left(-\frac{1}{2}\right) - 6 < 0$

$\Rightarrow$ lie on same side
So (2) true
Now for $2x+3y+6=0$

$A\left(1, \frac{1}{2}\right) \Rightarrow 2 + \frac{3}{2} + 6 > 0$

$\left(3, -\frac{1}{2}\right) \Rightarrow 6 - \frac{3}{2} + 6 > 0$

$\Rightarrow$ lie on same side
So (1)(2)(4) are true.

8. **Ans. (a)** $P(A\bar{B}) + P(\bar{A}B)$

$= \frac{40}{100} \cdot \frac{50}{100} + \frac{60}{100} \cdot \frac{50}{100}$

$\frac{2000 + 3000}{10000} = \frac{5000}{10000} = \frac{1}{2}$

9. **Ans. (c)** For CONTINUITY

$\lim_{x \to 0} f(x) = \lim_{x \to 0} x^2 \sin\frac{1}{x} = 0$. bounded=0

Also $f(0)=0 \Rightarrow f$ is continuous at $x=0$
Now differentiability .

$\lim_{x \to 0} \frac{f(x) - f(0)}{x - 0}$

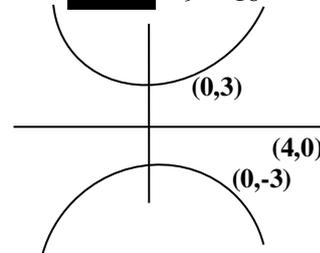$= \lim_{x \to 0} \frac{x^2 \sin\frac{1}{x} - 0}{x} = \lim_{x \to 0} x \sin\frac{1}{x} = 0$

$\Rightarrow f$ is diff. at x=0

$f' = \begin{cases} 2x\sin\frac{1}{x} + x^2 \cos\frac{1}{x}\left(-\frac{1}{x^2}\right), & x \neq 0 \\ 0, & x = 0 \end{cases}$

$= \begin{cases} 2x\sin\frac{1}{x} - \cos\frac{1}{x}, & x \neq 0 \\ 0 & x = 0 \end{cases}$

$f'(0^+) = 2x\sin\frac{1}{x} - \cos\frac{1}{x}\Big|_{x=0} = DNE$

10. **Ans. (c)** $\frac{y^2}{9} - \frac{x^2}{16} = 1$

(0,3)

(4,0)

(0,-3)

$\frac{x^2}{4} + \frac{(y-4)^2}{16} = 1 \Rightarrow \frac{Y^2}{16} + \frac{X^2}{4} = 1$

(0,4)
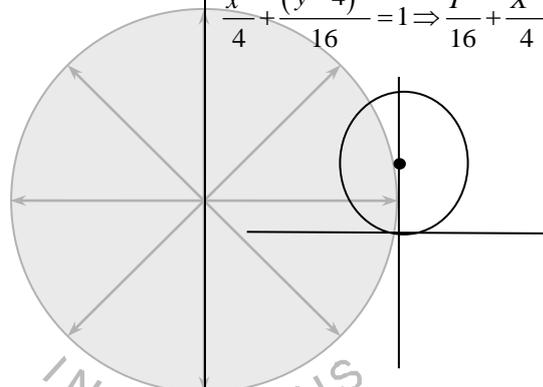
Nov $\frac{y^2}{9} - \frac{x^2}{16} = 1$ and $\frac{x^2}{4} + \frac{(y-4)^2}{16} = 1$

(0,4)

(0,3)
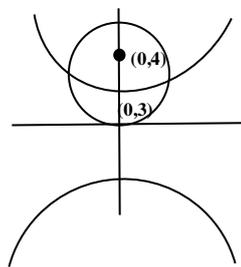
$\Rightarrow$ Two points of intersection

11. **Ans. (b)**

12. **Ans. (c)** Each parallel line among $L_2, L_4, L_6, L_8, L_{10}$ intersect each of L_1, L_3, L_5, L_7, L_9 in 5 points 50 total intersector between = $5 \times 5 = 25$

L_1 L_3 L_5
L_2 L_7
L_4 L_9
L_6
L_8
L_{10}
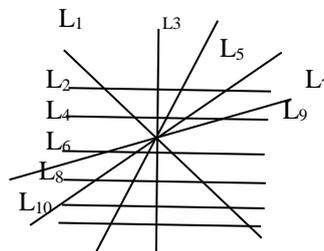
Also L_1, L_3, L_5, L_7, L_9 intersect at a point $\Rightarrow$ total interest points=25+1= 26

13. **Ans. (d)** $|[abc]| = \begin{vmatrix} m & 1 & 1 \\ 1 & -1 & 1 \\ 1 & 2 & -1 \end{vmatrix} = \pm 4$

m(1-2)-1(-2)+(3)= $\pm$ 4

-m+5= $\pm$ 4=4, -4

-m=-1,-9 $\Rightarrow$ m=1, 9

14. **Ans. (b)** $ax^2 + 2hxy + by^2 + 2x + 2f + y + c = 0$

Here $h^2 - ab < 0 \Rightarrow ellipse$

$\Delta \neq 0$

Now $3x^2 + 10xy + 11y^2 + 14x + 12y + 5 = 0$

a=3, h4=5, b=11, g=7, f=6, c=5

$h^2 - ab = 5^2 - 3.11 < 0$

$\Rightarrow ellipse$

15. **Ans. (c)** $f = x^{\frac{2}{3}}(r-x)^{\frac{1}{3}}$

$f' = \frac{2}{3}x^{-\frac{1}{3}}(6-x)^{\frac{1}{3}} + x^{\frac{2}{3}}\left(\dfrac{\frac{1}{3}(6-x)^{-\frac{2}{3}}}{-1}\right)$

$= \frac{2}{3}\dfrac{(6-x)^{1/3}}{x^{\frac{1}{3}}} - \frac{1}{3}\dfrac{x^{\frac{2}{3}}}{(6-x)^{\frac{2}{3}}}$

$\dfrac{2(6-x) - x}{3x^{\frac{1}{3}}(6-x)^{\frac{2}{3}}}$

$= \dfrac{12-3x}{3x^{\frac{1}{3}}(6-x)^{\frac{2}{3}}}$

$\Rightarrow f'(x)=0$ at x=6, 0, 4

16. **Ans. (b)** $\int\limits_0^3 e^{x^2}dx = \int\limits_0^5 e^{x^2}dx + \int\limits_5^3 e^{x^2}dx$

as $\int\limits_a^b f(x)dx = \int\limits_a^c f(x)dx + \int\limits_c^b f(x)dx$

17. **Ans. (d)** $f(x) = \dfrac{x}{e^{\pi x} - 1}$

$\lim\limits_{x\to 0}\dfrac{x}{e^{\pi x}-1} = \lim\limits_{x\to 0}\dfrac{\pi x}{e^{\pi x}-1}\times\dfrac{1}{\pi} = 1.\dfrac{1}{\pi} = \dfrac{1}{\pi}$

Also $f(0) = \dfrac{1}{\pi} \Rightarrow \lim\limits_{x\to 0} f(x) = f(0)$

$\Rightarrow$ f is continuous of x=0

Now to check differences

$\lim\limits_{x\to 0}\dfrac{f(x) - f(0)}{x - 0} = \lim\limits_{x\to 0}\dfrac{\dfrac{x}{e^{\pi x}-1} - \dfrac{1}{\pi}}{x}$

$= \lim\limits_{x\to 0}\dfrac{\pi x - (e^{\pi x} - 1)}{\pi x(e^{\pi x} - 1)} \to \dfrac{0}{0} \, for \, m$

$= \lim\limits_{x\to 0}\dfrac{\pi - e^{\pi x}.\pi}{\pi\left[(e^{\pi x} - 1) + xe^{\pi x}.\pi\right]}$

$= \lim\limits_{x\to 0}\dfrac{1 - e^{\pi x}}{e^{\pi x} - 1 + \pi xe^{\pi x}}$

$= \lim\limits_{x\to 0}\dfrac{-e^{\pi x}.\pi}{\pi e^{\pi x} + \pi e^{\pi x} + \pi^2 xe^{\pi x}}$

$\dfrac{-.\pi}{2.\pi} = -\dfrac{1}{2}$

18. **Ans. (a)** p(1,4), q(k,3)

Has mid point= $\left(\dfrac{k+1}{2}, \dfrac{7}{2}\right)$

And slope= $\dfrac{-1}{k-1} \Rightarrow$ slope of perpendicular=k-1

So equation of perpendicular bisector

$y - \dfrac{7}{2} = (k-1)\left(x - \left(\dfrac{k+1}{2}\right)\right)$

Now for y intercept x=0

$y - \dfrac{7}{2} = (k-1)\left(-\left(\dfrac{k+1}{2}\right)\right)$

$y - \dfrac{7}{2} = -\left(\dfrac{k^2-1}{2}\right)$

$y = 4 - \dfrac{k^2}{2} = -4$

$\Rightarrow 8 = \dfrac{k^2}{2} \Rightarrow k = \pm 4$

19. **Ans. (c)** Head will come half time

So $p = \dfrac{1}{2}$

20. **Ans. (b)** $^s P_3 = \dfrac{\underline{|5}}{\underline{|2}} = 60$

21. **Ans. (b)** $f\left(\dfrac{1-x}{1+x}\right) = x + 2$
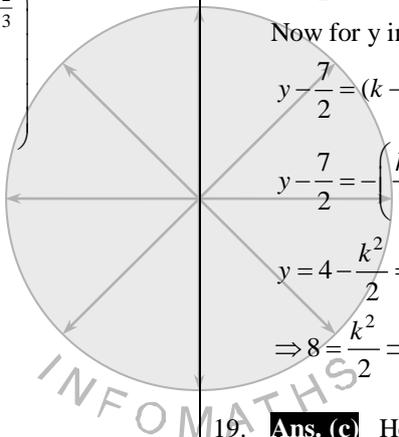
Take $\dfrac{1-x}{1+x} = y$

$\Rightarrow \dfrac{2}{-2x} = \dfrac{y+1}{y-1}$ by C and D

$x = \dfrac{1-y}{1+y}$

$\Rightarrow f\left(\dfrac{1-x}{1+x}\right) = x+2$ becomes

f(y)= $\dfrac{1-y}{1+y} + 2 = \dfrac{y+3}{y+1}$

$\Rightarrow f(1) = \dfrac{4}{2} = 2$

9

22. **Ans. (b)** COPLANER $\begin{vmatrix} \lambda^2 & 1 & 1 \\ 1 & \lambda^2 & 1 \\ 1 & 1 & \lambda^2 \end{vmatrix} = 0$

$\lambda^2(\lambda^4 - 1) - 1(\lambda^2 - 1) + (1 - \lambda^2) = 0$

$\lambda^2(\lambda^2 - 1)(\lambda^2 + 1) - 2(\lambda^2 - 1) = 0$

$(\lambda^2 - 1)(\lambda^2(\lambda^2 + 1) - 2) = 0$

$(\lambda^2 - 1)(\lambda^4 + \lambda^2 - 2) = 0$

$(\lambda^2 - 1)(\lambda^2 + 2)(\lambda^2 - 1) = 0$

$\Rightarrow \lambda^2 = 1, 1, -2$

$\Rightarrow \lambda^2 = 1 \Rightarrow$ distinct values

$\lambda = \pm 1$

23. **Ans. (a)** $w = Fs \cos\theta$

$180 \times 25 \cos 45°$

$= 4500 \times \dfrac{1}{\sqrt{2}}$

$\dfrac{45 \times \sqrt{2}}{2} \times 10^2$

$\dfrac{45 \times 1.4}{2} \times 10^2$

$= 45 \times 1.7 \times 10^2 = 31.5 \times 10^2$

$= 3.15 \times 10^3$ (approx)

24. **Ans. (a)** $\cos\left[\pi^2\right]x + \cos\left[-\pi^2\right]x = f(x)$

$\pi = 3.14 \Rightarrow \pi^2 = 9 \ldots\ldots$

$\Rightarrow \left[\pi^2\right] = 9, \left[-\pi^2\right] = -10$

$f\left(\dfrac{\pi}{2}\right) = \cos 9x + \cos(-10x)$

$= \cos 9x + \cos 10x$

$\Rightarrow f\left(\dfrac{\pi}{2}\right) = \cos\dfrac{9\pi}{2} + \cos\pi$

$= 0 - 1 = -1$

25. **Ans. (a)** $M_0 = 3M_i - 2\bar{x}$

$9^x = 3.3^x - 2$

$3^{2x} - 3.3^x + 2 = 0$

$t^2 - 3t + 2 = 0$

$\Rightarrow t = 1, 2$

$\Rightarrow 3^x = 1 \Rightarrow x = 0 \Rightarrow \text{mod} = 9^x = 9^0 = 1$

and $3^x = 2$

$\Rightarrow$ (Mode) $9^x = \left(3^x\right)^2 = 2^2 = 4$

26. **Ans. (d)** $w = Fs \cos\theta$

$= 40 \times 3 \times \cos 60°$

$= 120 \times \dfrac{1}{2} = 60$

27. **Ans. (a)** Solenoidal $\Rightarrow \quad \nabla.\vec{A} = 0$

$= \dfrac{\partial}{\partial x}(2x + 1) + \dfrac{\partial}{\partial y}\left(x^2 - 6y\right)$

$\dfrac{+\partial}{\partial z}\left(xy^2 + 3z\right) = 0$

$= 2 - 6 + 3 = 0$

$= -1 \Rightarrow div.\vec{A} = -ve \Rightarrow$ Sink field

28. **Ans. (a)** Let x, y be two numbers

$\dfrac{x + y}{2} = a \Rightarrow x, a, y \to$ A.P

$\Rightarrow 2a = x + y$

Also x, p, q, y $\to$ G.P

$\Rightarrow p^2 = xq \Rightarrow p^3 = xpq$

$q^2 = py \Rightarrow q^3 = pqy$

$\Rightarrow p^3 + q^3 = pq(x + y) = pq\,3r$

$= 2e\,pq$

29. **Ans. (a)** If married couple serve
$\Rightarrow {}^7C_3$

If married couple not serve $= {}^7C_5$

Probability $= \dfrac{{}^7C_3 + {}^7C_5}{{}^9C_5}$

$= \dfrac{35 + 21}{126} = \dfrac{56}{126} = \dfrac{4}{9}$

30. **Ans. (b)** No. divisible by 2,3 from 1 to 100
$= [6, 12, 18, \underline{}, 96]$

$= \dfrac{{}^{16}C_3}{{}^{100}C_3} = \dfrac{\dfrac{\lfloor 16}{\lfloor 3 \lfloor 13}}{\dfrac{\lfloor 100}{\lfloor 3 \lfloor 97}} = \dfrac{4}{1155}$

31. **Ans. (c)** $\Delta = 0 \Rightarrow \begin{vmatrix} 1 & 2 & 2 \\ 1 & 2 & 3 \\ 1 & 2 & \lambda \end{vmatrix} = 0$

$1(2\lambda - 6) - (2\lambda - 4) + (6 - 4) = 0$

$\dfrac{2\lambda}{\lambda} - 6 - \dfrac{2\lambda}{\lambda} + 4 + 2 = 0$

$\Delta_3 = \begin{vmatrix} 1 & 2 & 5 \\ 1 & 2 & 6 \\ 1 & 2 & \mu \end{vmatrix} = 0$

$\Rightarrow 1(2\mu - 12) - (2\mu - 10) + (12 - 10) = 0$

$0 = 0$

$\Delta_2 = \begin{vmatrix} 5 & 2 & 2 \\ 6 & 2 & 3 \\ \mu & 2 & \lambda \end{vmatrix} = 0$

$5(2\lambda - 6) - 6(2\lambda - 4) + \mu(2) = 0$

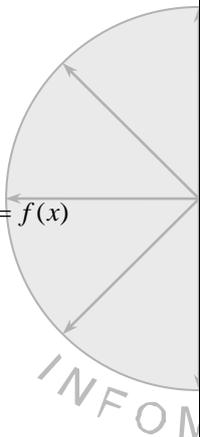$10\lambda - 30 - 12\lambda + 24 + 2\mu = 0$

$-2\lambda + 2\mu - 6 = 0$

$\lambda - \mu + 3 = 0$

from choices device only (c) satisfies.

32. **Ans. (d)** for invertible matrix

$|A| \neq 0$

So for not true.

$$\left| A\left(Adj A \right) \right| = \left| A \right| \left| Adj A \right|$$

$$= \left| A \right| \left| A \right|^{n-1} = \left| A \right|^n \neq 0$$

$$as \; \left| A \right| = 0 \Rightarrow \left| A(Adj A) \right| \neq 1 \text{ (need not be)}$$

33. **Ans. (d)** $\sin x = \sin y \Rightarrow \sin x - \sin y = 0$

$$\Rightarrow 2\cos\frac{x+y}{2} \sin\frac{x-y}{2} = 0$$

$$\Rightarrow 2\sin\frac{x+0}{2} \sin\frac{y-x}{2} = 0$$

For (1),(2) $\Rightarrow \sin(\frac{x-y}{2}) = 0$ or π

$$\Rightarrow \frac{x-y}{2} = 0 \text{ or } n\pi$$

$= x-y = 2\pi n$

34. **Ans. (c)** $\dfrac{2}{\sqrt{3}} + \dfrac{4}{\sqrt{5}} + \dfrac{6}{7} + \underline{\hspace{2cm}}$

$$= \sum_{n=1}^{\infty} \frac{2n}{\lfloor 2nx+1}$$

$$\sum_{n=1}^{\infty} \frac{(2n+1)-1}{\lfloor 2n+1}$$

$$= \int_{n=1}^{\infty} -\left(\frac{1}{\sqrt{2x}} - \frac{1}{\sqrt{2x+1}} \right)$$

$$= \left(\frac{1}{\lfloor 2} - \frac{1}{\lfloor 3} - \frac{1}{\lfloor 4} - \frac{1}{\lfloor 5} \underline{\hspace{1.5cm}} \right)$$

$$= e^{-1}$$

35. **Ans. (b)** $\sin 4x = \dfrac{1}{2} = \sin\dfrac{\pi}{6}$

$$4x = n\pi + (-1)^n \frac{\pi}{6}$$

$$x = \frac{n\pi}{4} + (-1)^n \frac{\pi}{24}$$

$$n=1 \Rightarrow x = \frac{\pi}{4} - \frac{\pi}{24} = \frac{5\pi}{24} < \frac{\pi}{2}$$

$$n=2 \Rightarrow x = \frac{\pi}{2} + \frac{\pi}{24} = \frac{13\pi}{24} > \frac{\pi}{2}$$

$$n=3 \Rightarrow x = \frac{3\pi}{4} - \frac{\pi}{24} = \frac{17\pi}{24} < \pi$$

$$n=4 \Rightarrow x = \pi + \frac{\pi}{24} > \pi$$

36. **Ans. (c)** For two perpendicular lines of $ax^2 + 2hxy + by^2 = 0$ condition is $a+b=0$

$$\Rightarrow 6x^2 - xy + \lambda y^2 = 0$$

$$\Rightarrow \lambda + 6 = 0$$

$$\Rightarrow \lambda = -6$$

Angle between of lines $\tan\theta \; 2\dfrac{\sqrt{h^2 - ab}}{a+b}$

$$= 2\frac{\sqrt{\left(-\frac{1}{2}\right)^2 - 6\lambda}}{6+\lambda} = \tan 45° = 1$$

$$2\sqrt{\frac{1}{4} - 6\lambda} = 6 + \lambda$$

$$4\left(\frac{1}{4} - 6\lambda \right) = 36 + \lambda^2 + 12\lambda$$

$$\lambda^2 + 36\lambda + 35 = 0$$

$$\lambda = -1, -35$$

$$\Rightarrow \lambda = -6, -35$$

37. **Ans. (c)**

$$5^{1+|\sin x| + |\sin x|^2 + \dots} = 25 = 5^2$$

$$\Rightarrow 1 + |\sin x| + |\sin x|^2 + \dots = 2$$

$$\frac{1}{1 - |\sin x|} = 2$$

$$\Rightarrow 1 - |\sin x| = \frac{1}{2}$$

$$|\sin x| = \frac{1}{2}$$

$$\Rightarrow \sin x = \pm\frac{1}{2}$$

$$x = \frac{\pi}{6}, \frac{5\pi}{6}$$

$$\frac{-\pi}{6}, \frac{-5\pi}{6}$$

38. **Ans. (d)** Combine median should be between two given medians.
$2 < m < 4$

39. **Ans. (a)** Here formula is

$$^nC_r \left[\frac{1}{\lfloor 2} - \frac{1}{\lfloor 3} + \frac{1}{\lfloor 4} + \underline{\hspace{1.5cm}} + \frac{(-1)^{n-r}}{\lfloor n-r} \right] \lfloor n-r$$

$$^9C_5 \left[\frac{1}{\lfloor 2} - \frac{1}{\lfloor 3} + \frac{1}{\lfloor 4} \right] \lfloor 4$$

$$= {}^9C_5 \left[\frac{12-4+1}{24} \right] \lfloor 4 = 9 \cdot {}^9C_5$$

40. **Ans. (a)** $^3C_2 (.6)^2 (.4)$
$3 \times (.36)(.4)$
$= .432$

41. **Ans. (d)**

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$$x = 3\cos 45° = \frac{3}{\sqrt{2}}$$

$$y = 3\sin 45° = \frac{3}{\sqrt{2}}$$

Maths online x = y in N-E direction Then walks north west direction distance of 4 units i.e. perpendicular to line x = y to point P

Now by distance form of line

$$\frac{x - \frac{3}{\sqrt{2}}}{\cos 41°} \frac{x - \frac{3}{\sqrt{2}}}{\cos 135°} = \frac{y - \frac{3}{\sqrt{2}}}{\sin 145°} = 4$$

$$\Rightarrow x = \frac{3}{\sqrt{2}} + 4\cos 135°, y = \frac{3}{\sqrt{2}} + 4\sin 135°$$

Continue : $\Rightarrow x = \frac{-1}{\sqrt{2}}, y = \frac{7}{\sqrt{2}}$

$$\Rightarrow \overrightarrow{OP} = \left(-\frac{1}{\sqrt{2}}\hat{i} + \frac{7}{\sqrt{2}}j\right)$$

42. **Ans. (b)** $f(x) = \begin{cases} -x^3 + 3x^2 + 1, & if\ x \le 2 \\ \cos(x), & if\ 2 < x \le 4 \\ e^{-x}, & if\ x > 4 \end{cases}$

$$f' = \begin{cases} -3x^2 + 6x, & x \le 2 \\ -\sin x, & 2 < x \le 4 \\ -e^{-x}, & x > 4 \end{cases}$$

$f' = 0 \Rightarrow -3x(x-2) = 0 \Rightarrow x = 0, 2$

also $5_{nx} = 0 \Rightarrow x = \pi$ as $2 < x \le 4$

$-e^x \ne 0$

$\Rightarrow$ only critical points are $0, 2, \pi$

$$f'' = \begin{cases} -6x + 6, & x \le 2 \\ -\cos x, & 2 < x \le 4 \\ +e^{-x}, & x > 4 \end{cases}$$

So f "(0)=6>0

$\Rightarrow$ x=0 is points of minimum

f "(2)=-6<0 $\Rightarrow$ x=2 is point of maxima

f "(π)=-cos π =1 $\Rightarrow$ x=π is point of minimum

Also for global MAX/MIN we check boundary points also

x = 2, 4

$\Rightarrow$ f(2)=-2^3+3.2^2+1=5

f(4)=cos 4 $\le$ 1

$\Rightarrow$ f(2) is point of absolute max also.

43. **Ans. (d)** $\tan\left(\frac{\pi}{4} + \theta\right)\tan\left(\frac{3\pi}{4} + \theta\right)$ is

$$\frac{1 + \tan\theta}{1 - \tan\theta} \cdot \frac{-1 + \tan\theta}{1 + \tan\theta} = -1$$

44. **Ans. (d)**

$$P\left(A \cap B^c\right) \cup \left(A^c \cap B\right)$$

$$P\left((A - B) \cup (B - A)\right)$$

$$= P(A) + P(B) - 2P(A \cap B)$$

45. **Ans. (c)**

$$\lim_{x \to 0} \frac{e^x - e^{-x} - 2x}{1 - \cos x}$$

$$\lim_{x \to 0} \frac{e^x + e^{-x} - 2}{\sin x} = \lim_{x \to 0} \frac{(e^x - 1) + (e^{-x} - 1)}{\sin x}$$

$$\lim_{x \to 0} \frac{\frac{e^x - 1}{x} + \frac{e^{-x} - 1}{x}}{\frac{\sin x}{x}} = \frac{1 - 1}{1} = 0$$

46. **Ans. (c)**

$x^2 - 2^y$

Here: (2, 2), (4, 4), (8, 6), (16, 8) etc. satisfies

So many infinitely many points satisfies.

47. **Ans. (b)** $y^2 = 4a(x + c)$

Normal to $y^2 = 4bx$

is $y = mx - 2bm - 4m^3$

Also normal to $y^2 = 4a(x + c)$

Is $y = m(m + c) - 2am - 4m^3$

$= mx + cm - 2am - 4m^3$

For(1), (2)

$$\frac{-2bm - 4m^3}{cm - 2am - 4m^3} = \frac{1}{1}$$

$-2bm - 4m^3 = cm - 2am - 4m^3$

$-2b = c - 29$

$\Rightarrow 2(a - b) < c$

48. **Ans. (d)**

Here 2a = PF + PF; FF = 2ae

$2a = \sqrt{4^2 + 3^2} + \sqrt{12^2 + 5^2} = 5 + 3 = 18,$

$\sqrt{(12 - 4)^2 + (5 - 3)^2} = 2ae$
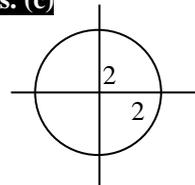
$\Rightarrow \sqrt{68} = 18e$

$e = \frac{\sqrt{17}}{9}$

49. **Ans. (b)**

$$\sum_{r=1}^{n} \frac{^nP_r}{2^n \lfloor r} = \sum_{r=1}^{n} \frac{^nC_r}{2^n} \text{ as } \frac{^nP_r}{\lfloor r} = {^nC_r}$$

$$= \frac{1}{2^a} \sum_{r=1}^{n} {^nC_r} = \frac{1}{2^n}\left[2^n - 1\right] = 1 - 2^{-n} \text{ as}$$

$$\sum_{r=0}^{n} {^nC_r} = 2^n$$

50. **Ans. (c)**

Now for a point (r, s), r > s is $\frac{1}{2}$